### RECSM Summer School: Social Media and Big Data Research

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Course website: pablobarbera.com/social-media-upf

# Supervised Machine Learning Applied to Social Media Text

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- Performance metric to choose best classifier and avoid overfitting: confusion matrix, accuracy, precision, recall...

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Relative disadvantage of supervised methods:

You *must* already know the dimension being scaled, because you have to feed it good sample documents in the training stage

Dictionary methods:

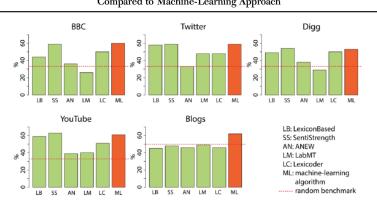
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- Supervised learning can be conceptualized as a generalization of dictionary methods, where features associated with each categories (and their relative weight) are learned from the data
- By construction, they will outperform dictionary methods in classification tasks, as long as training sample is large enough

### Dictionaries vs supervised learning



Lexicons' Accuracy in Document Classification Compared to Machine-Learning Approach

Source: González-Bailón and Paltoglou (2015)

How do we obtain a labeled set?

External sources of annotation

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  - Self-reported ideology in users' profiles

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- Crowd-sourced coding
  - Wisdom of crowds: aggregated judgments of non-experts converge to judgments of experts at much lower cost (Benoit et al, 2016)
  - Easy to implement with CrowdFlower or MTurk

#### Code the Content of a Sample of Tweets

Instructions -

In this job, you will be presented with tweets about the recent protests related to race and law enforcement in the U.S.

You will have to read the tweet and answer a set of questions about its content.

Read the tweet below paying close attention to detail:

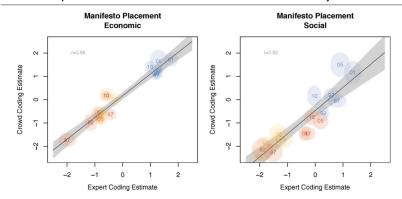
Tweet ID: 447



Is this tweet related to the ongoing debate about law enforcement and race in the United States?

- Yes
- O No
- O Don't Know

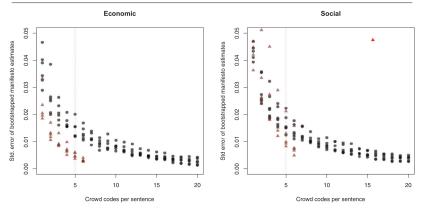
#### Crowd-sourced text analysis (Benoit et al, 2016 APSR)



#### FIGURE 3. Expert and Crowd-sourced Estimates of Economic and Social Policy Positions

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Note: Each point is the bootstrapped standard deviation of the mean of means aggregate manifesto scores, computed from sentencelevel random n subsamples from the codes.

## **Performance metrics**

Comasion matrix.	Actual label	
Classification (algorithm)	Negative	Positive
Negative	True negative	False negative
Positive	False positive	True positive

## **Performance metrics**

Confusion matrix

Actual label			
Negative	Positive		
True negative	False negative		
False positive	True positive		
TrueNeg + TruePos			
$rac{1}{3}$ + TruePos + FalseNeg + FalsePos			
Precision TruePos			
+ FalsePos			
Rocall TruePos			
+ FalseNeg			
	Negative True negative False positive TrueNeg + T g + TruePos + Fa uePos + FalsePos		

### Performance metrics: an example

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$$Accuracy = \frac{800 + 50}{700 + 50 + 100 + 50} = 0.85$$
$$Precision_{positive} = \frac{50}{50 + 50} = 0.50$$
$$Recall_{positive} = \frac{50}{50 + 100} = 0.33$$

Confusion matrix:

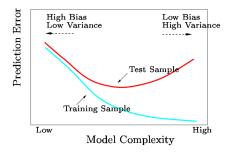
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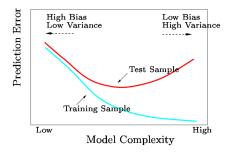
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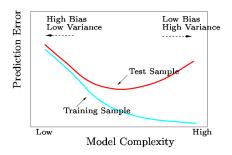
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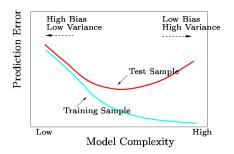


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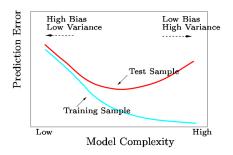
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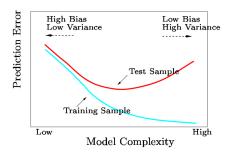
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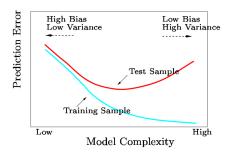
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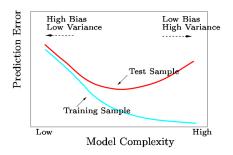
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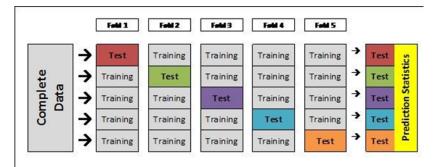
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  - Cross-validation

### **Cross-validation**

Intuition:

- Create K training and test sets ("folds") within training set.
- For each k in K, run classifier and estimate performance in test set within fold.
- Choose best classifier based on cross-validated performance



### Example: Theocharis et al (2016 JOC)

Why do politicians not take full advantage of interactive affordances of social media?

A politician's incentive structure

Democracy  $\rightarrow$  Dialogue > Mobilisation > Marketing Politician  $\rightarrow$  Marketing > Mobilisation > Dialogue\*

- H1: Politicians make broadcasting rather than engaging use of Twitter
- H2: Engaging style of tweeting is positively related to impolite or uncivil responses

### Data collection and case selection

Data: European Election Study 2014, Social Media Study

- List of all candidates with Twitter accounts in 28 EU countries
  - 2,482 out of 15,527 identified MEP candidates (16%)
- Collaboration with TNS Opinion to collect all tweets by candidates and tweets mentioning candidates (tweets, retweets, @-replies), May 5th to June 1st 2014.

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Case selection: expected variation in politeness/civility

	Received bailout	Did not receive bailout
High support for EU	Spain (55.4%)	Germany (68.5%)
Low support for EU	Greece (43.8%)	UK (41.4%)

(% indicate proportion of country that considers the EU to be "a good thing")

Data collection and case selection

#### Data coverage by country

Country	Lists	Candidates	on Twitter	Tweets
Germany	9	501	123 (25%)	86,777
Greece	9	359	99 (28%)	18,709
Spain	11	648	221 (34%)	463,937
UK	28	733	304 (41%)	273,886

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 $\label{eq:incivility} \textbf{Incivility} = \textbf{impoliteness} + \textbf{moral and democracy}$ 

Coding process: summary statistics				
	Germany	Greece	Spain	UK
Coded by 1/by 2	2947/2819	2787/2955	3490/1952	3189/3296
Total coded	5766	5742	5442	6485
Impolite	399	1050	121	328
Polite	5367	4692	5321	6157
% Agreement	92	80	93	95
Krippendorf/Maxwell	0.30/0.85	0.26/0.60	0.17/0.87	0.54/0.90
Broadcasting	2755	2883	1771	1557
Engaging	3011	2859	3671	4928
% Agreement	79	85	84	85
Krippendorf/Maxwell	0.58/0.59	0.70/0.70	0.66/0.69	0.62/0.70
Moral/Dem.	265	204	437	531
Other	5501	5538	5005	5954
% Agreement	95	97	96	90
Krippendorf/Maxwell	0.50/0.91	0.53/0.93	0.41/0.92	0.39/0.81

Coded tweets as training dataset for a machine learning classifier:

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- 3. Evaluate classifier: compute accuracy using 5-fold crossvalidation

#### Classifier performance (5-fold cross-validation)

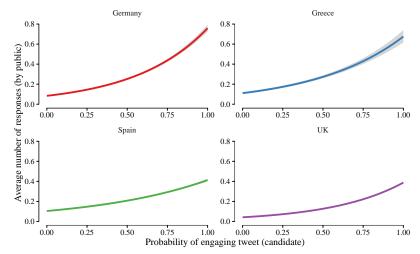
		UK	Spain	Greece	Germany
Communication	Accuracy	0.821	0.775	0.863	0.806
Style	Precision	0.837	0.795	0.838	0.818
	Recall	0.946	0.890	0.894	0.832
Polite vs.	Accuracy	0.954	0.976	0.821	0.935
impolite	Precision	0.955	0.977	0.849	0.938
	Recall	0.998	1.000	0.953	0.997
Morality and	Accuracy	0.895	0.913	0.957	0.922
Democracy	Precision	0.734	0.665	0.851	0.770
	Recall	0.206	0.166	0.080	0.061

#### Top predictive n-grams

Broadcasting	just, hack, #votegreen2014, :, and, @ ', tonight, candid, up, tonbridg, vote @, im @, follow ukip, ukip @, #telleu- rop, angri, #ep2014, password, stori, #vote2014, team, #labourdoorstep, crimin, bbc news
Engaging	@ thank, @ ye, you'r, @ it', @ mani, @ pleas, u, @ hi, @ congratul, :), index, vote # skip, @ good, fear, cheer, haven't, lol, @ i'v, you'v, @ that', choice, @ wa, @ who, @ hope
Impolite	cunt, fuck, twat, stupid, shit, dick, tit, wanker, scumbag, moron, cock, foot, racist, fascist, sicken, fart, @ fuck, ars, suck, nigga, nigga ?, smug, idiot, @arsehol, arsehol
Polite	@ thank, eu, #ep2014, thank, know, candid, veri, politi- cian, today, way, differ, europ, democraci, interview, time, tonight, @ think, news, european, sorri, congratul, good, :, democrat, seat
Moral/Dem.	democraci, polic, freedom, media, racist, gay, peac, fraud, discrimin, homosexu, muslim, equal, right, crime, law, vi- olenc, constitut, faith, bbc, christian, marriag, god, cp, racism, sexist
Others	@ ha, 2, snp, nice, tell, eu, congratul, campaign, leav, alreadi, wonder, vote @, ;), hust, nh, brit, tori, deliv, bad, immigr, #ukip, live, count, got, roma

### Predictive validity

# Citizens are more likely to respond to candidates when they adopt an engaging style

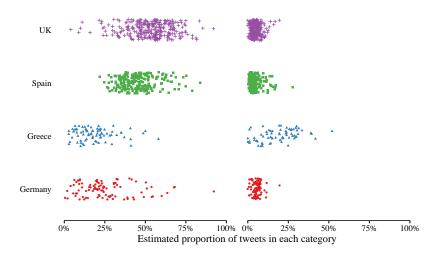


### Results: H1

# Proportion of engaging tweets sent and impolite tweets received, by candidate and country

Engaging (based on candidates)

Impolite (based on public)





Is engaging style positively related to impolite responses? Three levels of analysis:

#### Results: H2

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#### Results: H2

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- 2. Within candidates, over time: the number of impolite responses increases during the campaign for candidates who send more engaging tweets
- 3. Across tweets: tweets that are classified as engaging tend to receive more impolite responses

General thoughts:

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Frequently used classifiers:

Naive Bayes

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- Others: k-nearest neighbors, tree-based methods, etc.
- Ensemble methods

Assume we have:

- $i = 1, 2, \dots, N$  documents
- Each document *i* is in class  $y_i = 0$  or  $y_i = 1$
- $j = 1, 2, \ldots, J$  unique features
- And x<sub>ij</sub> as the count of feature j in document i

We could build a linear regression model as a classifier, using the values of  $\beta_0$ ,  $\beta_1$ , ...,  $\beta_J$  that minimize:

$$RSS = \sum_{i=1}^{N} \left( y_i - \beta_0 - \sum_{j=1}^{J} \beta_j x_{ij} \right)^2$$

But can we?

- If J > N, OLS does not have a unique solution
- Even with N > J, OLS has low bias/high variance (overfitting)

What can we do? Add a penalty for model complexity, such that we now minimize:

$$\sum_{i=1}^{N} \left( y_i - \beta_0 - \sum_{j=1}^{J} \beta_j x_{ij} \right)^2 + \lambda \sum_{j=1}^{J} \beta_j^2 \rightarrow \text{ridge regression}$$

or

$$\sum_{i=1}^{N} \left( y_i - \beta_0 - \sum_{j=1}^{J} \beta_j x_{ij} \right)^2 + \lambda \sum_{j=1}^{J} |\beta_j| \rightarrow \text{lasso regression}$$

where  $\lambda$  is the **penalty parameter** (to be estimated)

Why the penalty (shrinkage)?

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Evaluation: regularized regression is easy to interpret, but often outperformed by more complex methods.